Topological Superconductivity and Majorana Zero Modes in Superconductor-Semiconductor Hybrid Materials

> Charles Marcus Center for Quantum Devices, Niels Bohr Institute, University of Copenhagen

- 1) Topological superconductivity and Majorana zero modes in nanowires
- 2) Caution, skepticism, and what's going on
- 3) The pseudo-Zeeman route to topological superconductivity: super-semi-ferro
- 4) The vortex route to topological superconductivity: full-shell nanowires
- 5) The planar Josephson junction route to topological superconductivity









Unpaired Majorana fermions in quantum wires

A Yu Kitaev

<u>Abstract</u>. Certain one-dimensional Fermi systems have an energy gap in the bulk spectrum while boundary states are described by one Majorana operator per boundary point. A finite system of length L possesses two ground states with an energy difference proportional to $\exp(-L/l_0)$ and different fermionic parities. Such systems can be used as qubits since they are intrinsically immune to decoherence. The property of a system to have boundary Majorana fermions is expressed as a condition on the bulk electron spectrum. The condition is satisfied in the presence of an arbitrary small energy gap induced by proximity of a three-dimensional p-wave superconductor, provided that the normal spectrum has an odd number of Fermi points in each half of the Brillouin zone (each spin component counts separately).



[†] It appears that only a triplet (p-wave) superconductivity in the threedimensional substrate can effectively induce the desired pairing between electrons with the same spin direction — at least, this is true in the absence of spin-orbit interaction.



Majorana Fermions and a Topological Phase Transition in Semiconductor-Superconductor Heterostructures

Roman M. Lutchyn, Jay D. Sau, and S. Das Sarma Joint Quantum Institute and Condensed Matter Theory Center, Department of Physics, University of Maryland, College Park, Maryland 20742-4111, USA (Received 24 February 2010; published 13 August 2010)

PRL 105, 177002 (2010)	PHYSICAL	REVIEW	LETTERS	22 OCTOBER 2010
------------------------	----------	--------	---------	-----------------

Helical Liquids and Majorana Bound States in Quantum Wires

Yuval Oreg,¹ Gil Refael,² and Felix von Oppen³

¹Department of Condensed Matter Physics, Weizmann Institute of Science, Rehovot, 76100, Israel ²Department of Physics, California Institute of Technology, Pasadena, California 91125, USA ³Dahlem Center for Complex Quantum Systems and Fachbereich Physik, Freie Universität Berlin, 14195 Berlin, Germany (Received 16 March 2010; published 20 October 2010)

We show that the combination of spin-orbit coupling with a Zeeman field or strong interactions may lead to the formation of a helical electron liquid in single-channel quantum wires, with spin and velocity



1D Semiconductors: InAs Nanowire



M.H. Madsen, P. Krogstrup, J. Nygård, Univ. of Copenhagen

Growing Nanowires



PHYSICAL REVIEW B 84, 144522 (2011)

S

Majorana fermions in semiconductor nanowires

Tudor D. Stanescu,¹ Roman M. Lutchyn,² and S. Das Sarma³ Department of Physics, West Virginia University, Morgantown, West Virginia 26506, USA ²Station Q, Microsoft Research, Santa Barbara, California 93106-6105, USA tter Theory Center, Department of Physics, University of Maryland, College Park, Maryland 20742, USA ved 27 July 2011; revised manuscript received 27 September 2011; published 28 October 2011)

Zero-energy end states as signature of topological superconductor



PHYSICAL REVIEW B 84, 144522 (2011)

S

Majorana fermions in semiconductor nanowires

Tudor D. Stanescu,¹ Roman M. Lutchyn,² and S. Das Sarma³

¹Department of Physics, West Virginia University, Morgantown, West Virginia 26506, USA
²Station Q, Microsoft Research, Santa Barbara, California 93106-6105, USA
³Condensed Matter Theory Center, Department of Physics, University of Maryland, College Park, Maryland 20742, USA
(Received 27 July 2011; revised manuscript received 27 September 2011; published 28 October 2011)





Zero-bias peaks and splitting in an Al-InAs nanowire topological superconductor as a signature of Majorana fermions

Anindya Das[†], Yuval Ronen[†], Yonatan Most, Yuval Oreg, Moty Heiblum^{*} and Hadas Shtrikman





NATURE PHYSICS | VOL 8 | DECEMBER 2012

PHYSICAL REVIEW B 87, 241401(R) (2013)

Ś

Superconductor-nanowire devices from tunneling to the multichannel regime: Zero-bias oscillations and magnetoconductance crossover

H. O. H. Churchill,^{1,2} V. Fatemi,² K. Grove-Rasmussen,³ M. T. Deng,⁴ P. Caroff,⁴ H. Q. Xu,^{4,5} and C. M. Marcus^{3,*}



Spin-resolved Andreev levels and parity crossings in hybrid superconductor-semiconductor nanostructures

Eduardo J. H. Lee¹, Xiaocheng Jiang², Manuel Houzet¹, Ramón Aguado³, Charles M. Lieber² and Silvano De Franceschi^{1*}



Epitaxy of semiconductor-superconductor nanowires

P. Krogstrup^{1*}, N. L. B. Ziino¹, W. Chang¹, S. M. Albrecht¹, M. H. Madsen¹, E. Johnson^{1,2}, J. Nygård^{1,3*}, C. M. Marcus¹ and T. S. Jespersen^{1*}





Two-terminal charge tunneling: Disentangling Majorana zero modes from partially separated Andreev bound states in semiconductor-superconductor heterostructures

Christopher Moore,¹ Tudor D. Stanescu,² and Sumanta Tewari¹ ¹Department of Physics and Astronomy, Clemson University, Clemson, South Carolina 29634, USA ²Department of Physics and Astronomy, West Virginia University, Morgantown, West Virginia 26506, USA





Physical mechanisms for zero-bias conductance peaks in Majorana nanowires



PHYSICAL REVIEW RESEARCH 2, 013377 (2020)

Physical mechanisms for zero-bias conductance peaks in Majorana nanowires

Haining Pan I and S. Das Sarma Condensed Matter Theory Center and Joint Quantum Institute, Department of Physics, University of Maryland, College Park, Maryland 20742, USA



FIG. 7. (a) Tunneling conductance as a function of the magnetic field at a small transmission rate to the lead. The darker color indicates the smaller conductance. This experimental result is from Ref. [28]; (b) fine-tuning parameters to fit (a); The ZBCP is the ugly one with $\sigma_{\mu} = 1$ meV; (c) tunneling conductance as a function of the magnetic field. The redder color indicates the larger conductance. This experimental result is from Ref. [29]; (d) fine-tuning parameters to fit (d). The ZBCP is the ugly one with $\sigma_{\mu} = 1$ meV.

Single-Electron Charging of a Superconducting Island

D. V. Averin and Yu. V. Nazarov

Department of Physics, State University of New York, Stony Brook, New York 11794 and Institute of Nuclear Physics, Moscow State University, Moscow 119899 GSP, Russia (Received 3 March 1992)

We have calculated the quasiparticle current through a superconducting island in the Coulomb blockade regime. The current depends strongly on the parity of the total number of free electrons in the island. This dependence reflects the difference between ground-state properties of the superconductor with even and with odd number of electrons.

PACS numbers: 73.40.Gk, 72.10.Bg, 74.20.Fg







NATURE · VOL 365 · 30 SEPTEMBER 1993

Two-electron quantization of the charge on a superconductor

P. Lafarge, P. Joyez, D. Esteve, C. Urbina & M. H. Devoret



Exponential protection of zero modes in Majorana islands

S. M. Albrecht¹*, A. P. Higginbotham^{1,2}*, M. Madsen¹, F. Kuemmeth¹, T. S. Jespersen¹, J. Nygård¹, P. Krogstrup¹ & C. M. Marcus¹



Exponential protection of zero modes in Majorana islands

S. M. Albrecht¹*, A. P. Higginbotham^{1,2}*, M. Madsen¹, F. Kuemmeth¹, T. S. Jespersen¹, J. Nygård¹, P. Krogstrup¹ & C. M. Marcus¹





• Exponential convergence to zero-energy mode with 1/4-micron characteristic length.

• Zero modes located at ends of wire.

PHYSICAL REVIEW B **93**, 235431 (2016)

Conductance of a proximitized nanowire in the Coulomb blockade regime

B. van Heck,¹ R. M. Lutchyn,² and L. I. Glazman¹ ¹Department of Physics, Yale University, New Haven, Connecticut 06520, USA ²Station Q, Microsoft Research, Santa Barbara, California 93106-6105, USA (Received 31 March 2016; published 20 June 2016)





Thus, we find that in the Majorana regime (c) the position of the Coulomb blockade peaks, even if those are thermally broadened, can be used as a sensitive probe of the ground-state degeneracy splitting due to a finite length of a nanowire. In this sense, our finding corroborates the conclusions of Ref. [44].

Generic New Platform for Topological Quantum Computation Using Semiconductor Heterostructures

Jay D. Sau,¹ Roman M. Lutchyn,¹ Sumanta Tewari,^{1,2} and S. Das Sarma¹

¹Condensed Matter Theory Center and Joint Quantum Institute, Department of Physics, University of Maryland, College Park, Maryland 20742-4111, USA ²Department of Physics and Astronomy, Clemson University, Clemson, South Carolina 29634, USA (Received 17 July 2009; published 27 January 2010)



Spin-Polarized Electron Tunneling Study of an Artificially Layered Superconductor with Internal Magnetic Field: EuO-Al

P. M. Tedrow and J. E. Tkaczyk

Francis Bitter National Magnet Laboratory, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139

and

A. Kumar Physics Department, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139 (Received 3 February 1986)



FIG. 2. Measured tunneling conductance vs voltage for an EuO-Al/Al₂O₃/Al junction with an applied field of 0.44 T and a voltage splitting equivalent to 1.73 T.



FIG. 3. Observed values of B^* vs applied field B for two EuO-Al films. The magnetization $\mu_0 M$ for EuO from Ref. 8 is shown by the solid line.

Thin-Film Superconductor in an Exchange Field

X. Hao, J. S. Moodera, and R. Meservey

Francis Bitter National Magnet Laboratory, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139 (Received 14 December 1990)

Using the technique of spin-polarized tunneling, we studied tunnel junctions with EuS/Al bilayer electrodes. We found a large effective internal field in the Al film, which gives rise to extra Zeeman splitting in the superconducting quasiparticle density of states and which is attributed to the exchange interaction between the Eu ions and the Al conduction electrons. This exchange field, acting only on the electron spins, is inversely proportional to the thickness of the Al, causes no observable orbital depairing in the Al, and leads to a first-order transition to the normal state.





FIG. 4. The dependence of the saturation internal field on the Al film thickness.

PHYSICAL REVIEW MATERIALS 1, 054402 (2017)

Revealing the magnetic proximity effect in EuS/Al bilayers through superconducting tunneling spectroscopy

E. Strambini,^{1,*} V. N. Golovach,^{2,3,4} G. De Simoni,¹ J. S. Moodera,⁵ F. S. Bergeret,^{2,3,†} and F. Giazotto^{1,‡}

¹NEST Istituto Nanoscienze-CNR and Scuola Normale Superiore, I-56127 Pisa, Italy

²Centro de Fisica de Materiales (CFM-MPC), Centro Mixto CSIC-UPV/EHU, Manuel de Lardizabal 5, E-20018 San Sebastian, Spain

³Donostia International Physics Center (DIPC), Manuel de Lardizabal 4, E-20018 San Sebastian, Spain

⁴*IKERBASQUE, Basque Foundation for Science, Maria Diaz de Haro 3, E-48013 Bilbao, Spain*

⁵Department of Physics and Francis Bitter Magnet Laboratory, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139, USA (Received 30 June 2017; published 4 October 2017)



FIG. 1. Junction layout and tunneling spectroscopy of the first magnetization. (a) Sketch of the cross bar forming the $EuS(5)/Al(7)/Al_2O_3/Al(18)$ vertical tunnel junction (the thickness is in nanometers). The area of the junction is a square of $290 \times 290 \ \mu m^2$. (b) Evolution of the differential conductance, obtained from the numerical derivative of the *I*-*V* curves, as a function of the voltage drop (*V*) and in-plane magnetic field (*B*) during the first magnetization of the EuS layer. (c) Comparison between the differential conductance of the tunnel junction measured at zero field before (black curve) and after (red curve) the magnetization of the EuS layer. All the measurements were taken at 25 mK.



Signature of a pair of Majorana zero modes in superconducting gold surface states

Sujit Manna^{a,b,1}, Peng Wei^{c,1,2}, Yingming Xie^d, Kam Tuen Law^d, Patrick A. Lee^{a,2}, and Jagadeesh S. Moodera^{a,e,f,2}

^aDepartment of Physics, Massachusetts Institute of Technology, Cambridge, MA 02139; ^bDepartment of Physics, Indian Institute of Technology Delhi, 110 016 New Delhi, India; ^cDepartment of Physics and Astronomy, University of California, Riverside, CA 92521; ^dDepartment of Physics, Hong Kong University of Science and Technology, Hong Kong; ^eFrancis Bitter Magnet Laboratory, Massachusetts Institute of Technology, Cambridge, MA 02139 and ^fPlasma Science and Fusion Center Massachusetts Institute of Technology, Cambridge, MA 02139



ACS APPLIED MATERIALS & INTERFACES

Coherent Epitaxial Semiconductor—Ferromagnetic Insulator InAs/ EuS Interfaces: Band Alignment and Magnetic Structure

Yu Liu, Alessandra Luchini, Sara Martí-Sánchez, Christian Koch, Sergej Schuwalow, Sabbir A. Khan, Tomaš Stankevič, Sonia Francoual, Jose R. L. Mardegan, Jonas A. Krieger, Vladimir N. Strocov, Jochen Stahn, Carlos A. F. Vaz, Mahesh Ramakrishnan, Urs Staub, Kim Lefmann, Gabriel Aeppli, Jordi Arbiol, and Peter Krogstrup*





pubs.acs.org/NanoLett

Letter

Semiconductor–Ferromagnetic Insulator–Superconductor Nanowires: Stray Field and Exchange Field

Yu Liu,^{†,‡} Saulius Vaitiekėnas,^{‡,§} Sara Martí-Sánchez,^{||} Christian Koch,^{||} Sean Hart,^{⊥,#} Zheng Cui,^{⊥,∇} Thomas Kanne,[‡] Sabbir A. Khan,^{†,‡} Rawa Tanta,^{†,‡} Shivendra Upadhyay,^{‡,§} Martin Espiñeira Cachaza,^{†,‡} Charles M. Marcus,^{‡,§} Jordi Arbiol,^{||,○} Kathryn A. Moler,^{⊥,#,∇} and Peter Krogstrup^{*,†,‡}







pubs.acs.org/NanoLett

Letter

Semiconductor–Ferromagnetic Insulator–Superconductor Nanowires: Stray Field and Exchange Field

Yu Liu,^{†,‡} Saulius Vaitiekėnas,^{‡,§} Sara Martí-Sánchez,[¶] Christian Koch,[¶] Sean Hart,^{⊥,#} Zheng Cui,^{⊥,∇} Thomas Kanne,[‡] Sabbir A. Khan,^{†,‡} Rawa Tanta,^{†,‡} Shivendra Upadhyay,^{‡,§} Martin Espiñeira Cachaza,^{†,‡} Charles M. Marcus,^{‡,§} Jordi Arbiol,^{∥,O} Kathryn A. Moler,^{⊥,#,∇} and Peter Krogstrup^{*,†,‡}



Check for updates

Zero-bias peaks at zero magnetic field in ferromagnetic hybrid nanowires

S. Vaitiekėnas ^{1,2}, Y. Liu^{1,3}, P. Krogstrup^{1,3} and C. M. Marcus ^{1,2}







Check for updates

Zero-bias peaks at zero magnetic field in ferromagnetic hybrid nanowires

S. Vaitiekėnas^{1,2}, Y. Liu^{1,3}, P. Krogstrup^{1,3} and C. M. Marcus^{1,2}





Zero-bias tunneling conductance peaks at zero applied magnetic field


Turning off the ferromagnetic pseudo-Zeeman field removes the zero-bias peak



 φ . (b) Differential conductance, G, at φ roop bias as a function of partier gate vice 2. (c) G as a function of source-drain bias voltage, V, and V_C from weaklue dashed line in (b). (d) G as a function of V and compensated V_{BG} measured compensation gate voltages. (e, f) Similar to (d) for devices 3 and 4 as a funct respectively.

portant for a more detailed understanding of h. Within this picture, the estimated remalive field after returning to zero applied field $|=0\rangle| \sim 1.3$ T, consistent with previously values [28, 29]. Zeeman fields of > 1 T were found sufficient to induce topolog call superty in hybrid InAs wires without EnS [30]. We there is considerable device-to-device variance ical field. For instance, the critical field for ras 70 mT, as shown in Supplemental Fig0S4, to 50 mT for device 1 in Fig. 1. small changes in $V_{\rm C}$ to occupancy of any rost illustrated for device. $V_{\rm U}$ and $V_{\rm L}$ was not need measured along the dat function of $V_{\rm C}$ ranges to the open regimes, G sweeps at different $V_{\rm BC}$ Fig. S5. Bias spectra ducting gap $\Delta \sim 50 \,\mu$ extending from $V_{\rm C0}$ Hard (gap is considerably sm



Electrostatic effects and topological superconductivity in semiconductor-superconductor-magnetic insulator hybrid wires

Benjamin D. Woods and Tudor D. Stanescu Department of Physics and Astronomy, West Virginia University, Morgantown, WV 26506, USA



Microscopic analysis of topological superconductivity in ferromagnetic hybrid nanowires

Samuel D. Escribano,¹ Elsa Prada,² Yuval Oreg,³ and Alfredo Levy Yeyati¹

¹Departamento de Física Teórica de la Materia Condensada C5, Condensed Matter Physics Center (IFIMAC) and Instituto Nicolás Cabrera, Universidad Autónoma de Madrid, E-28049 Madrid, Spain ²Instituto de Ciencia de Materiales de Madrid (ICMM), Consejo Superior de Investigaciones Científicas (CSIC), E-28049 Madrid, Spain ³Department of Condensed Matter Physics, Weizmann Institute of Science, Rehovot, Israel 7610



Topological superconductivity in tripartite superconductor-ferromagnet-semiconductor nanowires

Josias Langbehn, Sergio Acero González, Piet W. Brouwer, and Felix von Oppen Dahlem Center for Complex Quantum Systems and Fachbereich Physik, Freie Universität Berlin, 14195 Berlin, Germany

Motivated by recent experiments searching for Majorana zero modes in tripartite semiconductor nanowires with epitaxial superconductor and ferromagnetic-insulator layers, we explore the emergence of topological superconductivity in such devices for paradigmatic arrangements of the three constituents. Accounting for the competition between magnetism and superconductivity, we treat superconductivity self consistently and describe the electronic properties, including the superconducting and ferromagnetic proximity effects, within a direct wave-function approach. We conclude that the most viable mechanism for topological superconductivity relies on a superconductor-semiconductor-ferromagnet arrangement of the constituents, in which spin splitting and superconductivity is only weakly affected by the ferromagnetic insulator.



 $V_{\rm LG} \bullet$

left

10 nm

20 nm



Chun-Xiao Liu,^{1, 2, *} Sergej Schuwalow,³ Yu Liu,³ Kostas Vilkelis,^{1, 2} A. L. R. Manesco,^{4, 2} P. Krogstrup,³ and Michael Wimmer^{1, 2}

¹Qutech, Delft University of Technology, Delft 2600 GA, The Netherlands. ²Kavli Institute of Nanoscience, Delft University of Technology, Delft 2600 GA, The Netherlands. ³Center for Quantum Devices, Niels Bohr Institute, University of Copenhagen and Microsoft Quantum Materials Lab Copenhagen, Lyngby, Denmark. ⁴Computational Materials Science Group (ComputEEL), Escola de Engenharia de Lorena, Universidade de São Paulo (EEL-USP),

Materials Engineering Department (Demar), Lorena – SP, Brazil

We study the electronic properties of InAs/EuS/Al heterostructures as explored in a recent ex-

• $V_{\rm RG}$

periment [S. Vaitiekėnas *et al.*, Nat. Phy microscopic device simulations. In particul investigate the band bending at the InAs/E essential input to subsequent microscopic de function distribution. We conclude that tl the InAs/EuS interfaces are both essential magnetic field. Mapping the topological pha induced exchange couplings, we show that and EuS layers can become a topological s that the topological phase can be optimized combined experimental and theoretical effo

EuS

40 nm

20 nm

 $V_{\rm BG}$

InAs

substrate backgate



subs

back

ate

ate

 $V_{\rm BG}$



-0.7 - 0.35 0.0

 $V_{\rm RG}$ (V)

0.35

PHYSICAL REVIEW B 105, L041304 (2022)

Evidence for spin-polarized bound states in semiconductor–superconductor–ferromagnetic-insulator islands

S. Vaitiekėnas,¹ R. Seoane Souto[®],^{1,2} Y. Liu[®],¹ P. Krogstrup,¹ K. Flensberg[®],¹ M. Leijnse[®],^{1,2} and C. M. Marcus[®],¹ ¹Center for Quantum Devices, Niels Bohr Institute, University of Copenhagen, 2100 Copenhagen, Denmark ²Division of Solid State Physics and NanoLund, Lund University, 22100 Lund, Sweden





PHYSICAL REVIEW B 105, L041304 (2022)

Evidence for spin-polarized bound states in semiconductor–superconductor–ferromagnetic-insulator islands

S. Vaitiekėnas,¹ R. Seoane Souto¹,^{1,2} Y. Liu¹,¹ P. Krogstrup,¹ K. Flensberg¹,¹ M. Leijnse¹,^{1,2} and C. M. Marcus¹ ¹Center for Quantum Devices, Niels Bohr Institute, University of Copenhagen, 2100 Copenhagen, Denmark ²Division of Solid State Physics and NanoLund, Lund University, 22100 Lund, Sweden



Fractional Quantum Hall Effect

theory:



Paired states of fermions in two dimensions with breaking of parity and time-reversal symmetries and the fractional quantum Hall effect

N. Read and Dmitry Green

Departments of Physics and Applied Physics, Yale University, P.O. Box 208120, New Haven, Connecticut 06520-8120 (Received 30 June 1999)

> To conclude, our main results are: (i) p-wave pairing in spinless or spin-polarized fermions in the weak-pairing phase leads to the properties also found in the FQHE in the MR states, and supports the ideas of nonabelian statistics as a robust property, at least in the case of a pure system. Such statistics will also occur for the vortices in such a p-wave state in general in charged superfluid



J. Alicea, *Rep. Prog. Phys.* **75**, 076501 (2012).

We note that a zero mode on a vortex in an *A*-phase *p*-wave paired state was first found in Ref. 68.

⁶⁸N.B. Kopnin and M.M. Salomaa, Phys. Rev. B **44**, 9667 (1991)

Experimental Detection of a Majorana Mode in the core of a Magnetic Vortex inside a Topological Insulator-Superconductor Bi₂Te₃/NbSe₂ Heterostructure

Jin-Peng Xu,¹ Mei-Xiao Wang,¹ Zhi Long Liu,¹ Jian-Feng Ge,¹ Xiaojun Yang,² Canhua Liu,^{1,5,*} Zhu An Xu,^{2,5} Dandan Guan,¹ Chun Lei Gao,¹ Dong Qian,¹ Ying Liu,^{1,3,5} Qiang-Hua Wang,^{4,5} Fu-Chun Zhang,^{2,5} Qi-Kun Xue,⁶ and Jin-Feng Jia^{1,5,†}



Vortex-Core Structure Observed with a Scanning Tunneling Microscope

H. F. Hess, R. B. Robinson, and J. V. Waszczak

AT&T Bell Laboratories, 600 Mountain Avenue, Murray Hill, New Jersey 07974 (Received 28 December 1989)



week ending 26 AUGUST 2011

Ş

Majorana Modes at the Ends of Superconductor Vortices in Doped Topological Insulators

Pavan Hosur,¹ Pouyan Ghaemi,^{1,2} Roger S. K. Mong,¹ and Ashvin Vishwanath^{1,2}

¹Department of Physics, University of California, Berkeley, California 94720, USA

²Materials Sciences Division, Lawrence Berkeley National Laboratory, Berkeley, California 94720, USA

(Received 24 December 2010; published 22 August 2011)



Evidence for Majorana bound states in an iron-based superconductor

Dongfei Wang^{1,2}*, Lingyuan Kong^{1,2}*, Peng Fan^{1,2}*, Hui Chen¹, Shiyu Zhu^{1,2}, Wenyao Liu^{1,2}, Lu Cao^{1,2}, Yujie Sun^{1,3}, Shixuan Du^{1,3,4}, John Schneeloch⁵, Ruidan Zhong⁵, Genda Gu⁵, Liang Fu⁶, Hong Ding^{1,2,3,4+}, Hong-Jun Gao^{1,2,3,4+}



0

High

Low

-4

2

Energy (meV)



Α



High

С

65

OBSERVATION OF QUANTUM PERIODICITY IN THE TRANSITION TEMPERATURE OF A SUPERCONDUCTING CYLINDER^{*}

W. A. Little^{\dagger} and R. D. Parks^{\ddagger}

Department of Physics, Stanford University, Stanford, California (Received May 10, 1962; revised manuscript received June 15, 1962)





Destruction of the Global Phase Coherence in Ultrathin, Doubly Connected Superconducting Cylinders

Y. Liu,* Yu. Zadorozhny, M. M. Rosario, B. Y. Rock, P. T. Carrigan, H. Wang

In doubly connected superconductors, such as hollow cylinders, the fluxoid is known to be quantized, allowing the superfluid velocity to be controlled by an applied magnetic flux and the sample size. The sample-size–induced increase in superfluid velocity has been predicted to lead to the destruction of super-conductivity around half-integer flux quanta. We report transport measurements in ultrathin Al and Au_{0.7}In_{0.3} cylinders verifying the presence of this destructive regime characterized by the loss of the global phase coherence and reveal a phase diagram featuring disconnected phase coherent regions, as opposed to the single region seen in larger superconducting cylinders studied previously.







14 DECEMBER 2001 VOL 294 SCIENCE

Magnetoresistance Oscillations of Superconducting Al-Film Cylinders Covering InAs Nanowires below the Quantum Critical Point

I. Sternfeld,^{1,*} E. Levy,¹ M. Eshkol,¹ A. Tsukernik,² M. Karpovski,¹ Hadas Shtrikman,³ A. Kretinin,³ and A. Palevski¹

¹School of Physics and Astronomy, Raymond and Beverly Sackler Faculty of Exact Sciences, Tel Aviv University, Tel Aviv 69978, Israel

²The Center for Nanoscience and Nanotechnology, Tel Aviv University, Tel Aviv 69978, Israel

³Department of Condensed Matter Physics, The Weizmann Institute of Scienece, Rehovot 76100, Israel (Received 24 January 2011; published 11 July 2011)

When odd multiples of half flux quanta thread a cylindrical superconducting shell with a diameter d shorter than the zero temperature coherence length $\xi(0)$, superconductivity is predicted to be destroyed. We show here that as d is reduced in comparison to $\xi(0)$ the resistance attains the normal state value, which seems to be temperature independent in the vicinity of half flux quanta. The data are in agreement with recent theoretical results.



TOPOLOGICAL MATTER

Flux-induced topological superconductivity in full-shell nanowires

S. Vaitiekėnas, G. W. Winkler, B. van Heck, T. Karzig, M.-T. Deng, K. Flensberg, L. I. Glazman, C. Nayak, P. Krogstrup, R. M. Lutchyn*, C. M. Marcus*



From Little-Parks to Destructive Regime





Mean-field theory of the destructive regime

$$\frac{C(n, \phi)}{C(0, 0)} \stackrel{\text{(1)}}{\xrightarrow{}} \stackrel{\text{(1)}}{\xrightarrow{}}$$

$$\ln\left(\frac{T_{C}(n,\phi)}{T_{C}(0,0)}\right) = \psi\left(\frac{1}{2}\right) - \psi\left(\frac{1}{2} + \frac{\alpha(n,\phi)}{2\pi T_{C}(n,\phi)}\right) + Dirty-limit coherence length$$

$$\phi) = \frac{\xi(0)^{2}}{\pi R^{2}} T_{C}(0,0) \left[4\left(n - \frac{\phi}{\phi_{0}}\right)^{2} + \frac{t^{2}}{R^{2}}\left(\frac{\phi^{2}}{\phi_{0}^{2}} + \frac{n^{2}}{3}\right)\right].$$

$$(2)$$

$$\alpha(n,\phi) = \frac{\xi(0)^{2}}{R^{2}} T_{C}(0,0) \left[4\left(n - \frac{\phi}{\phi_{0}}\right)^{2} + \frac{t^{2}}{R^{2}}\left(\frac{\phi^{2}}{\phi_{0}^{2}} + \frac{n^{2}}{3}\right)\right]$$

$$I_{C}(B) = I_{C}(0) \left(\frac{T_{C}(B)}{T_{C}(0)}\right)^{3/2}$$

$$Bardeen, RMP 1962$$

 $\overline{T_C}$

Compare experiment in the destructive regime









Spectroscopy of InAs nanowire with fluxoid-quantized boundary





Spectroscopy of InAs nanowire with fluxoid-quantized boundary



Non-Topological Nanowires (larger diameter)



TOPOLOGICAL MATTER

Flux-induced topological superconductivity in full-shell nanowires

S. Vaitiekėnas, G. W. Winkler, B. van Heck, T. Karzig, M.-T. Deng, K. Flensberg, L. I. Glazman, C. Nayak, P. Krogstrup, R. M. Lutchyn*, C. M. Marcus*

Theory of the topological phase



TOPOLOGICAL MATTER

Flux-induced topological superconductivity in full-shell nanowires

S. Vaitiekėnas, G. W. Winkler, B. van Heck, T. Karzig, M.-T. Deng, K. Flensberg, L. I. Glazman, C. Nayak, P. Krogstrup, R. M. Lutchyn*, C. M. Marcus*





Theory of Caroli-de Gennes-Matricon analogs in full-shell nanowires

Pablo San-Jose,¹ Carlos Payá,¹ C. M. Marcus,² S. Vaitiekėnas,² and Elsa Prada¹

¹Instituto de Ciencia de Materiales de Madrid, Consejo Superior de Investigaciones Científicas (ICMM-CSIC), Madrid, Spain ²Center for Quantum Devices, Niels Bohr Institute, University of Copenhagen, 2100 Copenhagen, Denmark (Dated: July 18, 2022)



Theory of Caroli-de Gennes-Matricon analogs in full-shell nanowires

Pablo San-Jose,¹ Carlos Payá,¹ C. M. Marcus,² S. Vaitiekėnas,² and Elsa Prada¹

¹Instituto de Ciencia de Materiales de Madrid, Consejo Superior de Investigaciones Científicas (ICMM-CSIC), Madrid, Spain ²Center for Quantum Devices, Niels Bohr Institute, University of Copenhagen, 2100 Copenhagen, Denmark (Dated: July 18, 2022)













Longer segments have very small even odd spacing





Comparing exponential and power-law splitting






Absence of supercurrent sign reversal in a topological junction with a quantum dot

J. Schulenborg and K. Flensberg D

Center for Quantum Devices, Niels Bohr Institute, University of Copenhagen, 2100 Copenhagen, Denmark

(Received 15 October 2019; revised manuscript received 6 January 2020; published 28 January 2020)

Experimental techniques to verify Majoranas are of current interest. A prominent test is the effect of Majoranas on the Josephson current between two wires linked via a normal junction. Here, we study the case of a quantum dot connecting the two superconductors and the sign of the supercurrent in the trivial and topological regimes under grand-canonical equilibrium conditions, explicitly allowing for parity changes due to, e.g., quasiparticle poisoning. We find that the well-known supercurrent reversal for odd occupancy of the quantum dot (π junction) in the trivial case does not occur in the presence of Majoranas in the wires. However, we also find this to be a mere consequence of Majoranas being zero energy states. Therefore, the lack of supercurrent sign reversal can also be caused by trivial bound states and is thus not a discriminating signature of Majoranas.





Quantum Dot Parity Effects in Trivial and Topological Josephson Junctions

D. Razmadze⁽⁾,^{1,2} E. C. T. O'Farrell,^{1,2} P. Krogstrup,^{1,3} and C. M. Marcus⁽⁾,² ¹Center for Quantum Devices, Niels Bohr Institute, University of Copenhagen, 2100 Copenhagen, Denmark

Center for Quantum Devices, Niels Bohr Institute, University of Copenhagen, 2100 Copenhagen, Denmark ²Microsoft Quantum Lab–Copenhagen, 2100 Copenhagen, Denmark ³Microsoft Quantum Materials Lab–Copenhagen, 2800 Kongens Lyngby, Denmark

(Received 24 May 2020; accepted 10 August 2020; published 8 September 2020)



Quantum Dot Parity Effects in Trivial and Topological Josephson Junctions

D. Razmadze^(D),^{1,2} E. C. T. O'Farrell,^{1,2} P. Krogstrup,^{1,3} and C. M. Marcus^(D),²

¹Center for Quantum Devices, Niels Bohr Institute, University of Copenhagen, 2100 Copenhagen, Denmark ²Microsoft Quantum Lab–Copenhagen, 2100 Copenhagen, Denmark ³Microsoft Quantum Materials Lab–Copenhagen, 2800 Kongens Lyngby, Denmark

(Received 24 May 2020; accepted 10 August 2020; published 8 September 2020)



(e)

10

8

4

Quantum Dot Parity Effects in Trivial and Topological Josephson Junctions

D. Razmadze^(b),^{1,2} E. C. T. O'Farrell,^{1,2} P. Krogstrup,^{1,3} and C. M. Marcus^(b),²

¹Center for Quantum Devices, Niels Bohr Institute, University of Copenhagen, 2100 Copenhagen, Denmark ²Microsoft Quantum Lab–Copenhagen, 2100 Copenhagen, Denmark ³Microsoft Quantum Materials Lab–Copenhagen, 2800 Kongens Lyngby, Denmark

(Received 24 May 2020; accepted 10 August 2020; published 8 September 2020)



Frustrated proximity effect needn't be topological (quantized)



topologically locked boundary condition (fluxoid quantization)







unlocked phase difference

Nonstandard symmetry classes in mesoscopic normal-superconducting hybrid structures

Alexander Altland and Martin R. Zirnbauer Institut für Theoretische Physik, Universität zu Köln, Zülpicherstrasse 77, 50937 Köln, Germany (Received 4 March 1996)



tation gap opens up and we arrive at the "boring" situation where the vicinity of the chemical potential is devoid of single-particle states. However, by tuning the phase difference of the order parameters of the two superconducting regions to the special value π , we can make the gap close. More generally, we expect quasiparticle excitations to exist right at the chemical potential whenever the phase shift incurred during Andreev reflection vanishes on average over the NS-interfacial region.

Superconducting Proximity Effect and Majorana Fermions at the Surface of a Topological Insulator

Liang Fu and C.L. Kane

Department of Physics and Astronomy, University of Pennsylvania, Philadelphia, Pennsylvania 19104, USA (Received 11 July 2007; published 6 March 2008)

We study the proximity effect between an *s*-wave superconductor and the surface states of a strong topological insulator. The resulting two-dimensional state resembles a spinless $p_x + ip_y$ superconductor, but does not break time reversal symmetry. This state supports Majorana bound states at vortices. We show that linear junctions between superconductors mediated by the topological insulator form a nonchiral one-dimensional wire for Majorana fermions, and that circuits formed from these junctions provide a method for creating, manipulating, and fusing Majorana bound states.



FIG. 1. (a) A STIS line junction. (b) Spectrum of a line junction for $W = \mu = 0$ as a function of momentum for various ϕ . The solid line shows the Andreev bound states for $\phi = \pi$. The dashed lines are for $\phi = 3\pi/4$, $\pi/2$, and $\pi/4$. The bound states for $\phi = 0$ merge with the continuum, indicated by the shaded region.

Two-dimensional epitaxial superconductor-semiconductor heterostructures: A platform for topological superconducting networks

J. Shabani,^{1,2} M. Kjaergaard,³ H. J. Suominen,³ Younghyun Kim,⁴ F. Nichele,³ K. Pakrouski,⁵ T. Stankevic,³ R. M. Lutchyn,⁶ P. Krogstrup,³ R. Feidenhans'l,³ S. Kraemer,⁷ C. Nayak,^{4,6} M. Troyer,⁵ C. M. Marcus,³ and C. J. Palmstrøm^{1,7,8}



Two-Dimensional Platform for Networks of Majorana Bound States

Michael Hell,^{1,2} Martin Leijnse,^{1,2} and Karsten Flensberg¹ ¹Center for Quantum Devices and Station Q Copenhagen, Niels Bohr Institute, University of Copenhagen, DK-2100 Copenhagen, Denmark ²Division of Solid State Physics and NanoLund, Lund University, Box 118, S-22100 Lund, Sweden (Received 5 September 2016; published 10 March 2017)



Topological Superconductivity in a Planar Josephson Junction



Benefits of Weak Disorder in One-Dimensional Topological Superconductors

Arbel Haim¹ and Ady Stern²

¹Walter Burke Institute for Theoretical Physics and the Institute for Quantum Information and Matter, California Institute of Technology, Pasadena, California 91125, USA ²Department of Condensed Matter Physics, Weizmann Institute of Science, Rehovot 7610001, Israel

(Received 13 September 2018; published 29 March 2019)

Majorana bound states are zero-energy modes localized at the ends of a one-dimensional (1D) topological superconductor. Introducing disorder usually increases the Majorana localization length, until eventually inducing a topological phase transition to a trivial phase. In this Letter, we show that in some cases weak disorder causes the Majorana localization length to *decrease*, making the topological phase more robust. Increasing the disorder further eventually leads to a change of trend and to a phase transition to a trivial phase. Interestingly, the transition occurs at $\xi_0 \gg l$, where *l* is the disorder mean free path, and ξ_0 is the localization length in the clean limit. Our results are particularly relevant to 1D topological superconductors formed in planar Josephson junctions.



Evidence of topological superconductivity in planar Josephson junctions

Antonio Fornieri^{1,10}, Alexander M. Whiticar^{1,10}, F. Setiawan², Elías Portolés Marín¹, Asbjørn C. C. Drachmann¹, Anna Keselman³, Sergei Gronin^{4,5}, Candice Thomas^{4,5}, Tian Wang^{4,5}, Ray Kallaher^{4,5}, Geoffrey C. Gardner^{4,5}, Erez Berg^{2,6}, Michael J. Manfra^{4,5,7,8}, Ady Stern⁶, Charles M. Marcus¹* & Fabrizio Nichele^{1,9}*



N A T U R E | www.nature.com/nature

RESEARCH LETTER

а

Topological superconductivity in a phase-controlled **RESEARCH** LETTER Josephson junction

Hechen Ren^{1,2}, Falko Pientka^{1,3}, Sean Hart^{1,4}, Andrew T. Pierce¹, Michael Kosowsky¹, Lukas Lunczer⁵, Raimund Schlereth⁵, Benedikt Scharf⁶, Ewelina M. Hankiewicz⁶, Laurens W. Molenkamp⁵, Bertrand I. Halperin¹ & Amir Yacoby¹*







 φ

Evidence of topological superconductivity in planar Josephson junctions

RESEARCH LETTER





N A T U R E | www.nature.com/nature

Evidence of topological superconductivity in planar Josephson junctions

 $G(2e^{2}/h)$ $G(2e^{2}/h)$ $G(2e^{2}/h)$ $G(2e^{2}/h)$ 0.2 0.15 0.25 0.15 0.15 0.4 0 0.05 0.05 0.1 0.1 *B*_⊥ (mT) *B*_⊥ (mT) B_{\perp} (mT) B_{\perp} (mT) B_{\perp} (mT) с <u>п 25</u> -0.25 0.25 -0.25 0 0.25 -0.25 0 0.25 -0.25 0.25 Δ 0.25 0 0 0.2 -0.2 0.15 0.15 0.15 $B_{\rm H} = 0$ $B_{\rm II} = 250 \, \rm mT$ $B_{\rm H} = 525 \,{\rm mT}$ $B_{\rm H} = 600 \, {\rm mT}$ V_{sd} (mV) 0 0 0 0 0 -0.2 -0.2 -0.15 -0.15 -0.15 $-\Phi_0$ -**Φ**0 -**Φ**₀ Φ_0 $\dot{\Phi}_0$ -Φ₀ $\dot{\Phi}_0$ Φ_0 Ò Ó $-\dot{\Phi}_0$ Φ_0 0 Ó 0 G (2e²/h) $B_{...} = 0$ $B_{\rm II} = 525 \, {\rm mT}$ *B*₁₁ = 775 mT 0.2 0.2 0.4 $\varphi = 0$ 0.4 $\varphi = 0$ ≪0.**¢** $\pi \Delta a$ $=hv_{\rm ff}$ $\sim \pi$ G (2e²/h)) سرح 10 0.1 0.2 ∕ ^{sq} 0.2 0.1 0 0 0 -0.2 0 0.25 0.75 -0.15 0 0.15 -0.1 0.1 -0.1 0 0.1 0 0.5 0 $V_{\rm sd}~({\rm mV})$ $V_{\rm sd}$ (mV) $V_{\rm sd}$ (mV) $B_{\parallel}(T)$

Antonio Fornieri^{1,10}, Alexander M. Whiticar^{1,10}, F. Setiawan², Elías Portolés Marín¹, Asbjørn C. C. Drachmann¹, Anna Keselman³, Sergei Gronin^{4,5}, Candice Thomas^{4,5}, Tian Wang^{4,5}, Ray Kallaher^{4,5}, Geoffrey C. Gardner^{4,5}, Erez Berg^{2,6}, Michael J. Manfra^{4,5,7,8}, Ady Stern⁶, Charles M. Marcus¹* & Fabrizio Nichele^{1,9}*

NATURE | www.nature.com/nature

RESEARCH

а

LETTER

Evidence of topological superconductivity in planar Josephson junctions

Antonio Fornieri^{1,10}, Alexander M. Whiticar^{1,10}, F. Setiawan², Elías Portolés Marín¹, Asbjørn C. C. Drachmann¹, Anna Keselman³, Sergei Gronin^{4,5}, Candice Thomas^{4,5}, Tian Wang^{4,5}, Ray Kallaher^{4,5}, Geoffrey C. Gardner^{4,5}, Erez Berg^{2,6}, Michael J. Manfra^{4,5,7,8}, Adv Stern⁶, Charles M. Marcus¹* & Fabrizio Nichele^{1,9}*

Save

= ACTIVE = SRQ = REMOTE

Output CH2 OUTPUT

0

Recall

ADDRESS BAUD PARITY OUEUE Setup

Phase diagram and Majorana hunting

B DISPLAT

Output CH1 OUTPUT

0

= AUX IN 3 = ±10 = AUX IN 4 = ±100

Auto

Expand

Display Rato

STANFORD RE

X noise # AUX IN 1 # AUX IN 2 Display

Ratio

Expand

= 12 dB = 18 dB = 24 dB = 57NC < 200 H

Slope ADd Style: = 5 = x100 = mV 5 = 2 = x10 = µV 1 1 x1 = cV 1



Θ

$$\begin{split} W_{\rm SI} \ll &\xi_{\rm S} \qquad \xi_{\rm S} = h v_{\rm F} / \pi \Delta \approx \\ I(t) \simeq I(V_{\rm sd}) + \frac{\partial I}{\partial V} \bigg|_{V_{\rm sd}} V_{\rm ac} \sin(\omega t) + \frac{1}{2} \frac{\partial^2 I}{\partial V^2} \bigg|_{V_{\rm sd}}^{\gamma_{\rm F}} \\ & \times [V_{\rm ac} \sin(\omega t)]^2 + \frac{1}{6} \frac{\partial^3 I}{\partial V^3} \bigg|_{V_{\rm sd}} [V_{\rm ac} \sin(\omega t)]^3. \end{split} \qquad I_{3\omega}(V_{\rm sd}) = -\frac{1}{24} \frac{\partial^3 I}{\partial V^3} \bigg|_{V_{\rm sd}} V_{\rm ac}^3 \propto -\frac{\partial^2 G}{\partial V^2} \bigg|_{V_{\rm sd}} \end{split}$$

Freq 90 • UNLOCK INTERNAL SOLICE SINE OUT

Phase +60' SNE = POS EDGE = NEG EDGE Trg REF IN

0 0 **RESEARCH LETTER**

а

REFE

Evidence of topological superconductivity in planar Josephson junctions

Antonio Fornieri^{1,10}, Alexander M. Whiticar^{1,10}, F. Setiawan², Elías Portolés Marín¹, Asbjørn C. C. Drachmann¹, Anna Keselman³, Sergei Gronin^{4,5}, Candice Thomas^{4,5}, Tian Wang^{4,5}, Ray Kallaher^{4,5}, Geoffrey C. Gardner^{4,5}, Erez Berg^{2,6}, Michael J. Manfra^{4,5,7,8}, Ady Stern⁶, Charles M. Marcus¹* & Fabrizio Nichele^{1,9}*

Phase diagram and Majorana hunting



RESEARCH

а

LETTER

Evidence of topological superconductivity in planar Josephson junctions



а

Antonio Fornieri^{1,10}, Alexander M. Whiticar^{1,10}, F. Setiawan², Elías Portolés Marín¹, Asbjørn C. C. Drachmann¹, Anna Keselman³, Sergei Gronin^{4,5}, Candice Thomas^{4,5}, Tian Wang^{4,5}, Ray Kallaher^{4,5}, Geoffrey C. Gardner^{4,5}, Erez Berg^{2,6}, Michael J. Manfra^{4,5,7,8}, Ady Stern⁶, Charles M. Marcus¹* & Fabrizio Nichele^{1,9}*

Phase diagram and Majorana hunting



Topological superconductivity in planar Josephson junctions: Narrowing down to the nanowire limit



A. Banerjee,¹ O. Lesser,² M. A. Rahman,¹ H.-R. Wang,^{2,3} M.-R. Li,^{2,3}
A. Kringhøj,¹ A. M. Whiticar,¹ A. C. C. Drachmann,¹ C. Thomas,^{4,5} T. Wang,^{4,5}
M. J. Manfra,^{4,5,6,7} E. Berg,² Y. Oreg,² Ady Stern,² and C. M. Marcus¹



A. Banerjee,¹ O. Lesser,² M. A. Rahman,¹ H.-R. Wang,^{2,3} M.-R. Li,^{2,3}
A. Kringhøj,¹ A. M. Whiticar,¹ A. C. C. Drachmann,¹ C. Thomas,^{4,5} T. Wang,^{4,5}
M. J. Manfra,^{4,5,6,7} E. Berg,² Y. Oreg,² Ady Stern,² and C. M. Marcus¹



A. Banerjee,¹ O. Lesser,² M. A. Rahman,¹ H.-R. Wang,^{2,3} M.-R. Li,^{2,3}
A. Kringhøj,¹ A. M. Whiticar,¹ A. C. C. Drachmann,¹ C. Thomas,^{4,5} T. Wang,^{4,5}
M. J. Manfra,^{4,5,6,7} E. Berg,² Y. Oreg,² Ady Stern,² and C. M. Marcus¹

Topological transition (theory)



A. Banerjee,¹ O. Lesser,² M. A. Rahman,¹ H.-R. Wang,^{2,3} M.-R. Li,^{2,3}
A. Kringhøj,¹ A. M. Whiticar,¹ A. C. C. Drachmann,¹ C. Thomas,^{4,5} T. Wang,^{4,5}
M. J. Manfra,^{4,5,6,7} E. Berg,² Y. Oreg,² Ady Stern,² and C. M. Marcus¹

The perforated wide leads





A. Banerjee,¹ O. Lesser,² M. A. Rahman,¹ H.-R. Wang,^{2,3} M.-R. Li,^{2,3}
A. Kringhøj,¹ A. M. Whiticar,¹ A. C. C. Drachmann,¹ C. Thomas,^{4,5} T. Wang,^{4,5}
M. J. Manfra,^{4,5,6,7} E. Berg,² Y. Oreg,² Ady Stern,² and C. M. Marcus¹

Phase dependence (experiment and theory)



A. Banerjee,¹ O. Lesser,² M. A. Rahman,¹ H.-R. Wang,^{2,3} M.-R. Li,^{2,3}
A. Kringhøj,¹ A. M. Whiticar,¹ A. C. C. Drachmann,¹ C. Thomas,^{4,5} T. Wang,^{4,5}
M. J. Manfra,^{4,5,6,7} E. Berg,² Y. Oreg,² Ady Stern,² and C. M. Marcus¹

Simultaneous zero-bias peaks at both ends of the device (not always).





A. Banerjee,¹ O. Lesser,² M. A. Rahman,¹ H.-R. Wang,^{2,3} M.-R. Li,^{2,3} A. Kringhøj,¹ A. M. Whiticar,¹ A. C. C. Drachmann,¹ C. Thomas,^{4,5} T. Wang,^{4,5} M. J. Manfra,^{4, 5, 6, 7} E. Berg,² Y. Oreg,² Ady Stern,² and C. M. Marcus¹



Persistence of topological regions

A. Banerjee,¹ O. Lesser,² M. A. Rahman,¹ H.-R. Wang,^{2,3} M.-R. Li,^{2,3}
A. Kringhøj,¹ A. M. Whiticar,¹ A. C. C. Drachmann,¹ C. Thomas,^{4,5} T. Wang,^{4,5}
M. J. Manfra,^{4,5,6,7} E. Berg,² Y. Oreg,² Ady Stern,² and C. M. Marcus¹

Prevalence of topological regions (theory)

μ_N =3.3 meV

0.5

 $\mu_{\rm N} = 1.5 \, {\rm meV}$

0.5

0.3

 $B_{||}(T)$

0.3

 $B_{||}(T)$

0.4

0.4



Andreev rectifier: A nonlocal conductance signature of topological phase transitions

T. Ö. Rosdahl,^{1,*} A. Vuik,^{1,†} M. Kjaergaard,^{2,3} and A. R. Akhmerov¹





Nonlocal Conductance Spectroscopy of Andreev Bound States: Symmetry Relations and BCS Charges

Jeroen Danon,¹ Anna Birk Hellenes,² Esben Bork Hansen,² Lucas Casparis,^{2,3} Andrew P. Higginbotham,^{2,3} and Karsten Flensberg¹



Conductance-Matrix Symmetries of a Three-Terminal Hybrid Device

G. C. Ménard,^{1,2} G. L. R. Anselmetti,^{1,2} E. A. Martinez,^{1,2} D. Puglia,^{1,2} F. K. Malinowski,^{1,2} J. S. Lee,³ S. Choi,⁴ M. Pendharkar,⁴ C. J. Palmstrøm,^{3,4,5} K. Flensberg,¹ C. M. Marcus,^{1,2} L. Casparis,^{1,2,*} and A. P. Higginbotham^[1,2,†]



Local and Nonlocal Transport Spectroscopy in Planar Josephson Junctions

A. Banerjee,¹ O. Lesser,² M. A. Rahman,¹ C. Thomas,³ T. Wang,³ M. J. Manfra,^{3,4} E. Berg,² Y. Oreg,² Ady Stern,² and C. M. Marcus¹



Local and Nonlocal Transport Spectroscopy in Planar Josephson Junctions

A. Banerjee,¹ O. Lesser,² M. A. Rahman,¹ C. Thomas,³ T. Wang,³ M. J. Manfra,^{3,4} E. Berg,² Y. Oreg,² Ady Stern,² and C. M. Marcus¹



Local and Nonlocal Transport Spectroscopy in Planar Josephson Junctions

A. Banerjee,¹ O. Lesser,² M. A. Rahman,¹ C. Thomas,³ T. Wang,³ M. J. Manfra,^{3,4} E. Berg,² Y. Oreg,² Ady Stern,² and C. M. Marcus¹



Fractional Josephson Vortices and Braiding of Majorana Zero Modes in Planar Superconductor-Semiconductor Heterostructures

Ady Stern¹ and Erez Berg^{1,2} ¹Department of Condensed Matter Physics, Weizmann Institute of Science, Rehovot, Israel 76100 ²Department of Physics and the James Frank Institute, University of Chicago, Chicago, Illinois 60637, USA



